Applied Differential Equations and Modeling

Homework 8

Due in class Tuesday, May 15

- 1. Find the solution of the given initial value problem and draw its graph.
 - (a) $y'' + 2y' + 2y = \delta(t \pi)$ with y(0) = 1, y'(0) = 0
 - (b) $y'' + y = \delta(t 2\pi) \cos t$ with y(0) = 0, y'(0) = 1
- 2. Find the Laplace transform of the given function.
 - (a) $\int_0^t (t-\tau)^2 \cos 2\tau \, d\tau$
 - (b) $\int_0^t e^{-(t-\tau)} \sin \tau \, d\tau$
- 3. Find the inverse Laplace transform using the convolution theorem.
 - (a) $F(s) = \frac{1}{s^4(s^2+1)}$
 - (b) $F(s) = \frac{G(s)}{s^2 + 1}$
- 4. In each of the following problems, express the total response in terms of the forced response (using a convolution integral) and the free response.
 - (a) $y'' + \omega^2 y = g(t)$ with y(0) = 0, y'(0) = 1
 - (b) $y'' + 3y' + 2y = \cos(\alpha t)$ with y(0) = 1, y'(0) = 0
- 5. Which of the following transfer functions corresponds to a BIBO-stable system?
 - (a) $H(s) = \frac{1}{(s+1)^2(s^2+1)}$
 - (b) $H(s) = \frac{1}{s^2 1}$
 - (c) $H(s) = \frac{1}{6+11s+6s^2+s^3}$