Calculus on Manifolds

(CO17-100261)

Fall Semester 2019

Up-to-date course information can be found on the course website http://math.jacobs-university.de/petrat/teaching/2019_fall_calculus_on_manifolds/

1 Official Course Description

This course is a first introduction to modern concepts in geometry and topology which are fundamental to specialization topics in Pure Mathematics. Topics include manifolds, differential forms, and Stokes theorem (on differential forms and retranslation into its classical formulation).

2 Contact Information

| Instructor: | Prof. Sören Petrat |
|-------------|--------------------------------------------------|
| Email: | s.petrat@jacobs-university.de |
| Office: | Research I, room 112 |
| TA: | Prabhat Devkota (p.devkota@jacobs-university.de) |

3 Time and Place

Wed 08:15 – 09:30, WH-4 Seminar

Thu 11:15 – 12:30, WH-4 Seminar

First class: September 4, 2019; last class: December 5, 2019 No classes on October 3 (German Unity Day) and October 31 (Reformation Day)

4 Textbooks

The class material is similar to the following textbook:

• J. L. Lee - Introduction to Smooth Manifolds

5 Exercises

Each week there will be an exercise sheet/homework assignment. These are an integral part of the coursework and working on the exercise sheets consistently is the best preparation for the exams!

- The solutions have to be handed in at the beginning of class.
- No late submissions are accepted.
- The three worst exercise sheets are not considered for grading, in order to compensate for sickness, late adding etc.
- It is encouraged to discuss the exercise sheets with your classmates (e.g., discuss how to come up with the solution or what the right way of approaching the problem is). On the other hand, the solutions must be written down and handed in individually! Copying the solutions from somebody else is a violation of Academic Integrity.

6 Exams

There will be two exams, a midterm and a final. The midterm will cover all material from the first half of the course and the final will cover all material with emphasis on the second half. More details will be announced. Note that this class uses gradescope for grading exams, see https://gradescope.com for more information. (Note that you can opt out of this by notifying the instructor.)

7 Grading

The final grade is weighted as follows:

| Homework: | 20% |
|-----------|-----|
| Midterm: | 30% |
| Final: | 50% |

Note: If the midterm grade is worse than the grade of the final, then only the grade of the final counts for both midterm and final.

8 Tentative Class Schedule

| Session | Date | Topic |
|---------|------------|----------------------------------------|
| 1 | Sep 4 | Smooth functions |
| 2 | Sep 5 | Inverse function theorem |
| 3 | Sep 11 | Bump functions, Sard's theorem |
| 4 | Sep 12 | Differentiable structures on manifolds |
| 5 | Sep 18 | Examples |
| 6 | Sep 19 | Groups on manifolds |
| 7 | Sep 25 | Diffeomorphisms |
| 8 | Sep 26 | Tangent space |
| 9 | Oct 2 | Submanifolds |
| | Oct 3 | German Unity Day |
| 10 | Oct 9 | Immersions, submersions, rank theorem |
| 11 | Oct 10 | Embeddings in Euclidean space |
| 12 | $Oct \ 16$ | Vector field and integral curves |
| 13 | Oct 17 | Tangent and cotangent bundle |
| 14 | Oct 23 | Vector bundles |
| | Oct 24 | Midterm Exam |
| 15 | Oct 30 | Multilinear algebra |
| | Oct 31 | Reformation Day |
| 16 | Nov 6 | Differential forms |
| 17 | Nov 7 | Differential forms |
| 18 | Nov 13 | Manifolds with boundary |
| 19 | Nov 14 | Integration on manifolds |
| 20 | Nov 20 | Integration on manifolds |
| 21 | Nov 21 | Stokes's theorem |
| 22 | Nov 27 | Lie groups |
| 23 | Nov 28 | Lie groups |
| 24 | Dec 4 | Lie groups |
| 25 | Dec 5 | Lie algebra |
| | TBA | Final Exam |