September 12, 2023

Constructor University Fall 2023

Operations Research

Homework 2

Due on September 20, 2023

Note: Your homework must be submitted via moodle (see the link on the class website) on the due day BEFORE THE TUTORIAL, i.e., before 20:45.

Problem 1 [10 points]

Find all solutions for the underdetermined linear system Ax = b, where

	(2)	2	-1	-4			(-5)	
A =	1	1	1	1	and \boldsymbol{b}	L	2	
	1	1	0	-1		0 =	-1	•
	$\backslash 1$	1	3	5 /			\ 8 /	/

Problem 2 [5 points]

Reconsider Problem 1 above: State at least two different basic solutions. Make sure that at least one of these is a basic *feasible* solution, i.e., a solution where all components are non-negative.

Problem 3 [5 points]

Reconsider Problem 1 from Homework Sheet 1: Minimize

$$Z = 8 x_1 + 12 x_2$$

subject to

$$5 x_1 + 2 x_2 \ge 20,$$

$$4 x_1 + 3 x_2 \ge 24,$$

$$x_2 \ge 2,$$

$$x_1, x_2 \ge 0.$$

Introduce slack variables to write this linear programming problem in the standard form: *Minimize*

$$Z = \boldsymbol{c}^T \boldsymbol{x}$$

subject to

$$A \boldsymbol{x} = \boldsymbol{b}$$

 $\boldsymbol{x} \ge 0$

where the coefficients $\boldsymbol{b}, \boldsymbol{c}$, and the decision variables \boldsymbol{x} are written as column vectors, and A is a matrix of matching dimension.