Conclusion from last time:  
We know how to compute all solutions to 
$$A \times = b$$
,  $A$  a nide matrix, in the  
specific form  $\times = \times^{basic} \star \times^{hom}$ , where  $\times^{hom}$  solves  $A \times^{hom} = 0$ , and  $\times^{basic}$  has at  
least as many 0 entries as "number of columns" ninus "number of pivots".  
 $=$  total number of variables in standard form  
CP problem, i.e.,  $\times \times \times_{in} \times_{$ 

How does the feasible region look like?  

$$A \times = b$$
 describes an affine subspace regin a plane in 3d.  
The feasible region is that part of the subspace with  $\times \ge 0$ !  
="quadrant" where all components are  
nonnegative (i.e., positive or  
E.g.:  
 $x_{e}$   
 $f_{easible}$  region has shape of a "simplex"

Important insight: If there is an optimal solution, we can always find one at a cornerpoint. And the cornerpoints correspond to the basic solutions of Ax=b. These we can find with bassian elimination.

A frescible region (ike in the picture could arise from 
$$_{1}e_{21,1} A = (5,3,4)$$
  
 $x_{1} x_{2} x_{1} x_{1}$   
 $x_{2} x_{1} x_{1} x_{1}$   
 $x_{2} and b = 2.$   
 $x_{2} composetion (1) = 2 (1)$ 

Proof idea:  
Suppose x is optimal, but not a converpoint. Then there is always a vector v such that both x+v and x-v are still feasible. In fact, since x minimizes 
$$c^{T}x$$
:  
 $\cdot c^{T}x \leq c^{T}(x+v) = c^{T}v \geq 0$   
 $\cdot c^{T}x \leq c^{T}(x-v) = c^{T}v \leq 0$   
so x+v and x-v are also optimal!